

Power-optimal Repeater Insertion Considering V_{dd} and V_{th} as Design Freedoms

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ABSTRACT

This work first presents an analytical repeater insertion method which optimizes power under delay constraint for a single net. This method finds the optimal repeater insertion lengths, repeater sizes, and V_{dd} and V_{th} levels for a net with a delay target, and it reduces more than 50% power over a previous work which does not consider V_{dd} and V_{th} optimization. This work further presents the power saving when multiple V_{dd} and V_{th} levels are used in repeater insertion at the full-chip level. Compared to the case with single V_{dd} and V_{th} suggested by ITRS, optimized dual V_{dd} and dual V_{th} can reduce overall global interconnect power by 47%, 28% and 13% for 130nm, 90nm and 65nm technology nodes, respectively, but extra V_{dd} or V_{th} levels only give marginal improvement. We also analyze the trends of V_{dd} and V_{th} optimization for chip level power reduction, and show that an optimized single V_{th} can reduce interconnect power almost as effective as dual- V_{th} does.

1. INTRODUCTION

Repeater insertion is extensively used in nowadays designs for delay reduction in long interconnect, which causes increasingly severe problem of power consumption due to the ever increasing number of repeaters [1]. Traditional approach of repeater insertion optimizes the interconnect in terms of delay, but several works in the literature [2, 3, 4] have made use of the extra tolerable delay (i.e., slack) in nets for significant saving in interconnect power. [2, 3] provide analytical methods to compute unit length power optimal repeater insertion solutions. [4] defines a new figure of merit which allows trade-off between power and delay using repeater insertion lengths, repeater sizes and wire widths as design knobs. None of the above work consider supply voltage V_{dd} and threshold voltage V_{th} as design freedoms. [5] performs dual V_{dd} and dual V_{th} assignments on logic circuits to reduce power consumption, and shows that 20% of power can be saved by going from single V_{th} to dual V_{th} under the dual V_{dd} power supply.

This paper studies the opportunity of power saving by computing power optimal repeater sizes, repeater insertion lengths, and for the first time V_{dd} and V_{th} levels for both individual nets and full chips. Our first contribution derives a set of analytical formulae which finds the optimal interconnect power given the amount of the timing slack on a single net. Our results show that more than 50% of power saving can be achieved over [2] which does not consider V_{dd} and V_{th} as design variables. Our second contribution studies the power saving of using multiple V_{dd} and V_{th} levels for buffering interconnects. Compared to the case without V_{dd} and V_{th}

optimization, optimized dual V_{dd} and dual V_{th} can reduce overall global interconnect power by 47%, 28% and 13% for 130nm, 90nm and 65nm technology nodes, respectively, but extra V_{dd} or V_{th} level only gives marginal improvement. We also analyze the trends of V_{dd} and V_{th} optimization for chip level power reduction, and show that an optimized single V_{th} can reduce interconnect power almost as effective as dual- V_{th} does.

This paper is organized as follows. Section 2 discusses the delay and the power models. Section 3 presents single-net power optimization with V_{dd} and V_{th} tuning. Section 4 studies the full chip power optimization using multiple V_{dd} and V_{th} . We conclude in Section 5.

2. PRELIMINARIES

This section discusses the delay and power models used in this paper. Both the delay and power models are based on those in [2], which assume fixed V_{dd} and V_{th} . We extend the models to reflect the effects of V_{dd} and V_{th} scaling.

2.1 Delay Model

Consider an interconnect segment of unit length resistance r and unit length capacitance c . It is driven by a repeater of size s with unit driving resistance r_s , unit input capacitance c_p and unit output capacitance c_o . We assume that the interconnect is terminated at the other end with another repeater of identical size. Suppose the interconnect segment is of length l , the delay of the driving repeater and the wire segment is

$$\tau = r_s(c_o + c_p) + \frac{r_s}{s}cl + r_lsc_o + \frac{1}{2}rcl^2 \quad (1)$$

and the unit length delay is

$$\frac{\tau}{l} = \frac{1}{l}r_s(c_o + c_p) + \frac{r_s}{s}c + r_lsc_o + \frac{1}{2}rcl \quad (2)$$

In Equation (2), the driving strength of a repeater depends on the operating V_{dd} and V_{th} levels and the driving resistance can be approximated in [3] by

$$r_s = K_1 \frac{V_{dd}}{I_{dsat}} \quad (3)$$

where K_1 is a fitting parameter and I_{dsat} is the saturated drain current of a minimum-sized NMOS or PMOS transistor with both V_{gs} and V_{ds} equal to V_{dd} . According to the alpha-power law model [6], I_{dsat} is modeled as

$$\begin{aligned} I_{dsat} &= K_2(V_{gs} - V_{th})^\alpha \\ &= K_2(V_{dd} - V_{th})^\alpha \end{aligned} \quad (4)$$

where K_2 is a device parameter and α typically equals to 1.25. By plugging Equation (4) into Equation (3), we obtain r_s as a function of V_{dd} and V_{th} .

$$r_s = K_3 \frac{V_{dd}}{(V_{dd} - V_{th})^\alpha} \quad (5)$$

where $K_3 = K_1/K_2$. For a given V_{dd} and V_{th} , the unit length delay is optimal when

$$l_{opt} = \sqrt{\frac{2r_s(c_o + c_p)}{rc}} \quad s_{opt} = \sqrt{\frac{r_s c}{rc_o}} \quad (6)$$

which results in the optimum unit length delay given by

$$\left(\frac{\tau}{l}\right)_{opt} = 2\sqrt{r_s c_o r c} \left(1 + \sqrt{\frac{1}{2} \left(1 + \frac{c_p}{c_o}\right)}\right) \quad (7)$$

When the delay target is larger than $(\frac{\tau}{l})_{opt}$, we can find a family of solutions $\{V_{dd}, V_{th}, l, s\}$ that satisfy the target delay [2]. In the solution set, there exists a solution that achieves the minimum power. The methodology of finding such solution is presented in Section 3.

2.2 Power Model

The power dissipation of a repeater comprises three parts: dynamic, leakage, and short circuit. We use the same formulae to compute power as in [2] except that V_{dd} and V_{th} are taken out of the constant coefficients and are treated as variables in the expressions. The power models are summarized below.

Dynamic power is the power dissipated when repeaters charge and discharge their loading capacitances. It is given by

$$P_{switching} = a(s(c_o + c_p) + lc)V_{dd}^2 f_{clk}$$

where a is the switching activity of a repeater, which is assumed to be 0.15, and f_{clk} is the clock frequency.

For the leakage power, we consider only the subthreshold leakage as in [2]. The subthreshold leakage current of a minimum-sized NMOS transistor is given by

$$I_{off} = I_{off}^{ref} \cdot 10^{\frac{(V_{th}^{ref} - V_{th})}{S_w}}$$

where I_{off}^{ref} and V_{th}^{ref} are some reference subthreshold leakage current and threshold voltage respectively for a technology, and S_w is the subthreshold swing, which we assume 100mV/decade at the temperature 100°C. The model assumes that the transistor is at OFF state when $V_{gs} = 0$ and $V_{ds} = V_{dd}$. For the ease of calculation, we change the formula from base 10 to base e and get

$$I_{off} = I_{off}^{ref} \cdot e^{\frac{(V_{th}^{ref} - V_{th})}{S_w}}$$

where $S_w' = \frac{S_w}{\log_e 10}$.

The average leakage power of a repeater is

$$\begin{aligned} P_{leakage} &= V_{dd} I_{leakage} \\ &= \frac{1}{2} V_{dd} (I_{off}^n W_{nmin} + I_{off}^p W_{pmin}) s \end{aligned}$$

where I_{off}^n and I_{off}^p are the reference subthreshold leakage current for NMOS and PMOS transistors respectively, and W_{min}^n and W_{min}^p are the widths of the NMOS and PMOS transistors in a minimum-sized inverter.

The short circuit power dissipation depends on the transition time at the input and the output of an inverter. Assuming symmetric high-to-low and low-to-high transitions at the input and the output of the

repeater, the short circuit power is given by

$$P_{short-circuit} = a t_r V_{dd} W_{min}^n s I_{short-circuit} f_{clk}$$

where a is the same switching factor as in the dynamic power expression, and $t_r = \tau \log_e 3$.

The total power is given by

$$P_{repeater} = P_{dynamic} + P_{leakage} + P_{short-circuit}$$

Therefore, we have

$$P_{repeater} = k_1 V_{dd}^2 (s(c_p + c_o) + lc) + k_2 V_{dd} e^{\frac{(V_{th}^{ref} - V_{th})}{S_w}} s + k_3 V_{dd} s \tau$$

where

$$\begin{aligned} k_1 &= a f_{clk} \\ k_2 &= \frac{1}{2} (I_{off}^n W_{min}^n + I_{off}^p W_{min}^p) \\ k_3 &= a W_{min}^n f_{clk} \log_e 3 \end{aligned}$$

and

$$\frac{P_{repeater}}{l} = k_1 \left(\frac{s}{l}(c_p + c_o) + c\right) + k_2 \frac{s}{l} + k_3 V_{dd} s \frac{\tau}{l} \quad (8)$$

We specify the target delay by using $(\frac{\tau}{l})_{opt}(1+f)$, where f is the slack expressed in terms of the extra fraction of optimal unit length delay. By setting the net delay $\tau = (1+f)(\frac{\tau}{l})_{opt} l$, we can simplify the expression by replacing $k_3 \frac{\tau}{l}$ with $k_3' = k_3(1+f)(\frac{\tau}{l})_{opt}$.

3. SINGLE NET POWER OPTIMIZATION

For an interconnect of length L , the total power dissipated by the inserted repeaters is $\frac{P_{repeater}}{l} L$, where $\frac{P_{repeater}}{l}$ is a function of $\{V_{dd}, V_{th}, l, s\}$. Given a delay target specified in terms of f , the objective is to select from the feasible solutions the one which gives the minimum total power dissipation for the wire. Therefore, the problem can be formulated mathematically as

$$\begin{aligned} \min \quad & \left(\frac{P_{repeater}}{l}\right) (V_{dd}, V_{th}, l, s) \\ \text{subject to} \quad & \left(\frac{\tau}{l}\right) (V_{dd}, V_{th}, l, s) = (1+f)(\frac{\tau}{l})_{opt} \end{aligned} \quad (9)$$

In this section, we first review the method from [2], which solves Problem (9) with pre-defined V_{dd} and V_{th} levels. Then we show that there exists a unique solution for Problem (9) and present a set of equations to solve the problem analytically. Finally we compare the results from power optimization with and without considering V_{dd} and V_{th} as optimization variables.

3.1 Optimization under fixed Vdd and Vth

For given V_{dd}, V_{th} , and a delay target, the optimal l and s that give the minimum $\frac{P_{repeater}}{l}$ can be obtained by solving the following set of nonlinear equations in [2], i.e.,

$$\frac{\partial \frac{P_{repeater}}{l}}{\partial s} = 0 \quad (10)$$

$$\left(\frac{\tau}{l}\right) (V_{dd}, V_{th}, l, s) - (1+f)(\frac{\tau}{l})_{opt} = 0 \quad (11)$$

The insertion length l is a function of the repeater size s under the equality delay constraint (11). In this problem, both the objective function and the constraint are posynomials. This type of problem is known to have a single local optimum that is also global, which can be obtained by setting the gradient of the objective function with respect to the design variables to zero.

3.2 Optimization with Vdd and Vth Tuning

When V_{dd} and V_{th} are treated as variables, the functions are no longer posynomials. Therefore it is not clear whether there is only one local optimum. The new problem can be solved by an exhaustive search on V_{dd} and V_{th} for the minimum power. For given V_{dd} and V_{th} , we obtain the minimum unit length power using the method in Section 3.1. Then we search on V_{dd} and V_{th} for the minimum $\frac{P_{repeater}}{l}$. Figure 1 shows the resulting contour plot of $\frac{P_{repeater}}{l}$ versus V_{dd} and V_{th} . Each contour line represents the continuous combination of V_{dd} and V_{th} that achieves the same value of $\frac{P_{repeater}}{l}$. The optimal value, which is a single point degenerated from a contour, locates right by the delay constraint line and is marked as $(V_{dd}^{opt}, V_{th}^{opt})$ in Figure 1. This plot shows

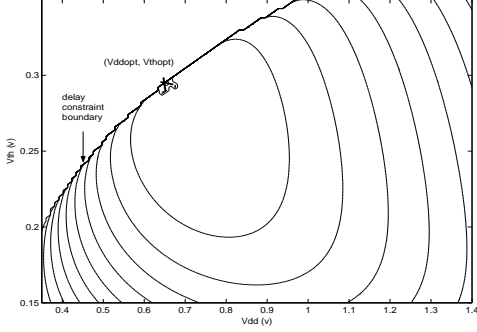


Figure 1: Contour plot of unit length power with Vdd and Vth as variables. The delay penalty is 5% of the optimal delay.

that there exists a unique optimum in the possible range of V_{dd} and V_{th} , which hints that the problem of power minimization through V_{dd} and V_{th} can be solved analytically. Our future research will attempt to prove that this problem possesses a unique local optimum. On the other hand, based on the observation from the exhaustive search, we develop an efficient analytical method below to solve this problem. The analytical and exhaustive search methods obtain the same results in all our experiments.

In order to solve for the optimal point directly, we derive a set of nonlinear equations by setting the gradient of the objective function to zero. Following the equality delay constraint, one of the variable must be a function of the other three variables. In our derivation, V_{th} is chosen to be the dependent variable, because it is the only variable that can be easily expressed in the closed-form of the other three variables. From Equation (5), V_{th} can be expressed in terms of V_{dd} and r_s as

$$V_{th} = V_{dd} - \left(\frac{K_3 V_{dd}}{r_s} \right)^{\frac{1}{\alpha}}$$

By rearranging Equation (2), r_s can be expressed as a function of l and s :

$$r_s = \frac{(1+f)(\frac{\tau}{l})_{opt} - rsc_o - \frac{1}{2}rcl}{\frac{c_o + c_p}{l} + \frac{c}{s}}$$

Therefore, when deriving the gradients of the objective function, V_{th} is treated as a function of V_{dd} , l and s . The following equations set the gradients of the objective function with respect to V_{dd} , s and

l to zero.

$$\begin{aligned} \frac{\partial \frac{P_{repeater}}{l}}{\partial V_{dd}} &= 2k_1 V_{dd} \left(\frac{s}{l} (c_o + c_p) + c \right) \\ &+ k_2 e^{\frac{-V_{th}(V_{dd}, l, s)}{S'_w}} \frac{s}{l} \\ &- \frac{1}{S'} \frac{\partial V_{th}}{\partial V_{dd}} k_2 V_{dd} e^{\frac{-V_{th}(V_{dd}, l, s)}{S'_w}} \frac{s}{l} + k'_3 s = 0 \end{aligned}$$

$$\begin{aligned} \frac{\partial \frac{P_{repeater}}{l}}{\partial s} &= k_1 V_{dd}^2 \frac{c_o + c_p}{l} \\ &+ k_2 V_{dd} e^{\frac{-V_{th}(V_{dd}, l, s)}{S'_w}} \frac{1}{l} \\ &- \frac{1}{S'} \frac{\partial V_{th}}{\partial s} k_2 V_{dd} e^{\frac{-V_{th}(V_{dd}, l, s)}{S'_w}} \frac{s}{l} + k'_3 V_{dd} = 0 \end{aligned}$$

$$\begin{aligned} \frac{\partial \frac{P_{repeater}}{l}}{\partial l} &= -k_1 V_{dd}^2 (c_o + c_p) \frac{s}{l^2} \\ &- k_2 V_{dd} e^{\frac{-V_{th}(V_{dd}, l, s)}{S'_w}} \frac{s}{l^2} \\ &- \frac{1}{S'} \frac{\partial V_{th}}{\partial l} k_2 V_{dd} e^{\frac{-V_{th}(V_{dd}, l, s)}{S'_w}} \frac{s}{l} = 0 \end{aligned}$$

where

$$\begin{aligned} \frac{\partial V_{th}}{\partial V_{dd}} &= 1 - \frac{1}{\alpha} \left(\frac{K_3}{r_s} \right)^{\frac{1}{\alpha}} V_{dd}^{\frac{1}{\alpha} - 1} \\ \frac{\partial V_{th}}{\partial s} &= \frac{1}{\alpha} (K_3 V_{dd})^{\frac{1}{\alpha}} r_s^{-\frac{1}{\alpha} - 1} \frac{\partial r_s}{\partial s} \\ \frac{\partial V_{th}}{\partial l} &= \frac{1}{\alpha} (K_3 V_{dd})^{\frac{1}{\alpha}} r_s^{-\frac{1}{\alpha} - 1} \frac{\partial r_s}{\partial l} \end{aligned}$$

and

$$\begin{aligned} \frac{\partial r_s}{\partial s} &= \left(\frac{c_o + c_p}{l} + \frac{c}{s} \right)^{-2} \left\{ \frac{c}{s^2} \left((1+f) \left(\frac{\tau}{l} \right)_{opt} - \frac{1}{2} rcl \right) \right. \\ &\quad \left. - \frac{rcc_o}{s} - rc \left(\frac{c_o + c_p}{l} + \frac{c}{s} \right) \right\} \\ \frac{\partial r_s}{\partial l} &= -\frac{1}{2} rc \left(\frac{c_o + c_p}{l} + \frac{c}{s} \right)^{-1} \\ &+ \left\{ \frac{c_o + c_p}{l^2} \left((1+f) \left(\frac{\tau}{l} \right)_{opt} - rsc_o - \frac{1}{2} rcl \right) \right\} \\ &\quad \cdot \left(\frac{c_o + c_p}{l} + \frac{c}{s} \right)^{-2} \end{aligned}$$

These equations can be solved numerically using a standard nonlinear equation solver. We implement this in Matlab by using the command “fsolve”.

3.3 Experimental Results

The methodology proposed is used to optimize unit length power for a single net. The parameters for the power and delay models across various technology nodes up to 65nm are taken from [1]. Table 1 compares the proposed method to the method using fixed V_{dd} and V_{th} in Section 3.1 respectively across different technology for target delay $\tau = (1+f)(\frac{\tau}{l})_{opt}$ where f is between 5% and 100%. The results from optimization under fixed V_{dd} and V_{th} are called the reference values in this paper. The reference supply voltage V_{dd}^{ref} used for each technology are obtained from [1] and V_{th}^{ref} values are assumed to be 25% of their respective V_{dd}^{ref} as in [2].

As shown in Table 1, the amount of power saving that can be achieved from V_{dd} and V_{th} optimization depends on the delay target. For $f = 20\%$, the power saving is up to 28% across all technology nodes. When $f = 100\%$, the power saving is more than 50% for

node	f	V_{dd} (V)	$\frac{V_{dd}}{V_{dd}^{ref}}$	V_{th} (V)	$\frac{V_{th}}{V_{th}^{ref}}$	s (\times min)	$\frac{s}{s_{ref}}$	l (mm)	$\frac{l}{l_{ref}}$	$(\frac{P}{T})_{opt}$ (W/m)	$(\frac{P}{T})_{opt}$ saving
130	5%	1.06	0.92	0.27	0.95	59.5	1.12	1.65	0.97	0.16	3 %
	10%	0.97	0.82	0.27	0.95	59.7	1.31	1.74	0.93	0.13	10 %
	20%	0.84	0.70	0.26	0.95	59.1	1.61	1.92	0.92	0.10	25 %
	100%	0.51	0.41	0.24	0.85	42.1	2.60	3.13	1.01	0.04	62 %
90	5%	0.93	0.87	0.23	0.88	57.5	1.12	1.34	0.97	0.25	6 %
	10%	0.85	0.78	0.23	0.88	57.6	1.31	1.41	0.94	0.21	14 %
	20%	0.73	0.66	0.22	0.88	57.0	1.60	1.56	0.92	0.16	28 %
	100%	0.43	0.38	0.19	0.75	40.2	2.54	2.59	1.06	0.06	65 %
65	5%	0.75	1.02	0.20	1.12	39.4	1.08	0.87	0.96	0.23	2 %
	10%	0.69	0.92	0.20	1.11	39.4	1.25	0.92	0.92	0.20	7 %
	20%	0.60	0.79	0.20	1.10	39.0	1.51	1.03	0.89	0.16	18 %
	100%	0.36	0.45	0.16	0.91	27.9	2.35	1.77	0.99	0.07	54 %

Table 1: Unit length power solutions from optimization with Vdd and Vth tuning and the comparison with optimization under fixed V_{dd} and V_{th} .

all generations. The power saving is mainly achieved by lowering the supply voltage. As we can see, the optimal V_{dd} levels are generally lower than the reference values. The V_{dd} level decreases with increasing slack f , showing that V_{dd} provides good trade-off for power by utilizing f . The optimal V_{th} values slowly decreases with increasing f to compensate for the loss of performance from V_{dd} reduction. The reduction in V_{th} causes a moderate increase in leakage power, but is rewarded by a large decrease in the dynamic power from lowering V_{dd} . Repeater sizes s are larger than the reference values to compensate for the loss of the drive strength due to V_{dd} reduction. The segment lengths, l , stay relatively close to the reference values in all cases.

4. FULL-CHIP INTERCONNECT POWER

In this section, we propose a methodology to evaluate full-chip interconnect power. In [7], a closed-form analytical expression of the wire-length distribution for on-chip random logic networks based on Rent's rule is developed. We estimate the full-chip power by integrating the unit length power over the wire-length distribution from the smallest wire length with non-negligible power to the longest global interconnect assumed by the wire-length distribution model. We use the delay optimal segment length l_{opt} given by Equation (6) to define the shortest interconnect that requires repeater insertion. Nets shorter than l_{opt} are not considered as they do not need repeaters. The delay of each net is bounded by 90% of the clock period T_{clk} as in [8]. For an interconnect of length L operating at V_{dd} and V_{th} , the optimal delay is

$$D_{opt} = \left(\frac{\tau}{l}\right)_{opt} (V_{dd}, V_{th})L$$

where $(\frac{\tau}{l})_{opt}(V_{dd}, V_{th})$ is given by Equations (5) and (7). The difference between D_{opt} and $0.9 \cdot T_{clk}$ is the slack that we can use to optimize its power. We define L_{max} to be the longest interconnect length which satisfies the target delay with delay optimal repeater insertion, i.e.,

$$L_{max} = \frac{0.9 \cdot T_{clk}}{\left(\frac{\tau}{l}\right)_{opt}}$$

We pipeline the interconnects of lengths larger than L_{max} so that the length of each segment is smaller than L_{max} . We assume that the delay overhead of pipelining flip-flops is amortized in $0.1 \cdot T_{clk}$. Therefore, the power for the full-chip is given by

$$P = \int_{\nu_{opt}}^{2\sqrt{N}} \mathbf{R}(\nu) \left(\frac{P}{l}\right)_{opt} (f) l_{\beta} \beta d\nu \quad (12)$$

where

- ν wire length in terms of gate pitches;
- ν_{opt} l_{opt} in terms of gate pitches;
- N number of logic gates;
- β number of pipelining stages;
- l_{β} wire length per stage;
- $\mathbf{R}(\nu)$ wirelength distribution function;
- $\left(\frac{P}{l}\right)_{opt}(f)$ power per length function defined in the Problem Formulation (9);
- f slack in terms of multiple of $\left(\frac{\tau}{l}\right)$;

The length in terms of gate pitches is obtained by

$$\nu = \frac{l}{\sqrt{AF\mathbf{T}}} \quad (13)$$

where AF is the gate area factor, which is 320 across all technology nodes and \mathbf{T} is the technology node in terms of minimum local metal's half-pitch dimension. The number of pipelining stages β and the wire length per stage l_{β} are given by

$$\beta = \left\lceil \frac{\nu \sqrt{AF\mathbf{T}}}{L_{max}} \right\rceil,$$

$$l_{\beta} = \frac{\nu \sqrt{AF\mathbf{T}}}{\beta}$$

The optimal power per length $\left(\frac{P}{l}\right)_{opt}$ is a function of the target delay, and is obtained using the method discussed in Section 3.1 when V_{dd} and V_{th} are fixed and that in Section 3.2 when V_{dd} and V_{th} are design variables. Target delay of an interconnect of length l_{β} is again specified by $\tau = (1 + f) \left(\frac{\tau}{l}\right)_{opt} (V_{dd}, V_{th}) l_{\beta}$, where

$$f = \frac{0.9 \cdot T_{clk}}{\left(\frac{\tau}{l}\right)_{opt} \cdot l_{\beta}} - 1$$

Technology Node (nm)	130	90	65	45
# transistors (M)	97	193	276	1546
T_{clk} (ps)	594	251	148	86.9
V_{dd} (V)	1.1	1	0.7	0.6
V_{th} (V)	0.28	0.25	0.17	0.15
L_{max} (mm)	6.94	2.30	1.06	0.513
l_{opt} (mm)	1.32	1.06	0.67	0.540

Table 2: List of parameters based on 2001 ITRS.
Note: The number of gates N is assumed to be # transistors/4

4.1 Vdd and Vth Optimization

To optimize the full-chip interconnect power, we consider various cases of V_{dd} and V_{th} assignment for nets. Practical assignment has

limited number of V_{dd} and V_{th} levels throughout the chip. Multiple V_{dd} levels are provided either by having multiple power distribution networks or by inserting pass transistors to create lower V_{dd} supplies than the system V_{dd} . Multiple V_{th} can be achieved either through selective transistor doping or through substrate biasing. The V_{dd} and V_{th} pair for a net can be formed from any one of the available V_{dd} and V_{th} levels. Therefore, increasing V_{dd} and V_{th} levels improves the power saving it can achieve due to more fine-grained control to V_{dd} and V_{th} for each net. We are interested in maximizing the power saving that can be achieved by the minimum number of V_{dd} and V_{th} levels available at the full-chip level, since extra V_{dd} and V_{th} levels increase area and manufacturing costs. We compare the optimal full-chip global interconnect power of each combination (N_{dd}, N_{th}), where N_{dd} is the number of V_{dd} levels and N_{th} is the number of V_{th} levels. The theoretical optimum power occurs at $N_{dd} \rightarrow \infty$ and $N_{th} \rightarrow \infty$, i.e., the V_{dd} and V_{th} of each net can be tailored. Such comparison provides us with an idea of the potential power saving by increasing N_{dd} and N_{th} .

Table 3 shows our searching algorithm for the power optimal V_{dd} and V_{th} levels at the full-chip level. Given N_{dd} and N_{th} , the algorithm first generates all possible combinations of V_{dd} and V_{th} for the full-chip at line 3. For a particular N_{dd} levels of V_{dd} and N_{th} levels of V_{th} , any combination of (V_{dd}, V_{th}) that has lower delay per length than the reference combination $(V_{dd}^{ref}, V_{th}^{ref})$, which provides the best delay performance, is discarded. Combinations which cannot even achieve the delay bound at the shortest wire length $l_{opt}(V_{dd}^{ref}, V_{th}^{ref})$ in our defined global interconnect are also discarded. These are implemented in line 5. The algorithm then evaluates $L_{max}(V_{dd}, V_{th})$, which is the maximum wire length that satisfies the $0.9 \cdot T_{clk}$ delay bound, for every (V_{dd}, V_{th}) combination. The combinations are then sorted as in line 6, such that the nets of different lengths are assigned with V_{dd} and V_{th} as illustrated in Figure 2. Finally, the power of each of these regions with different (V_{dd}, V_{th}) assignments are computed in lines 9–14. Note that wires of length larger than $L_{max}(V_{dd}^{ref}, V_{th}^{ref})$ have to be broken down into segments by means of pipelining as discussed, which is implemented by looping on the number of pipeline stages at line 10 and by folding the integration bounds in lines 11–12. ν is simply the length in terms of gate pitches, and the conversion between ν and length in absolute dimensions are done using Equation (13). Also note that the optimal power per length function $(\frac{P}{T})(f, V_{dd}, V_{th})_{opt}$ in line 13 refers to the power optimal repeater insertion with fixed V_{dd} and V_{th} discussed in Section 3.1.

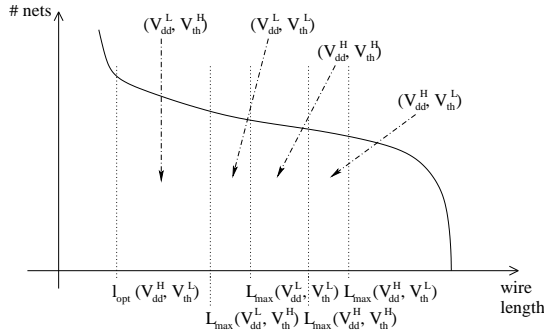


Figure 2: (V_{dd}, V_{th}) assignment in a net distribution

The ideal case in which $N_{dd} \rightarrow \infty$ and $N_{th} \rightarrow \infty$ can be computed by the same algorithm with some modification. Even though some smart pruning has been done to the search space as shown in Table 3, the algorithm fundamentally performs exhaustive

Algorithm: $ComputeOptPower(N_{dd}, N_{th})$	
1.	$S(V_{dd}) =$ the set of V_{dd} levels to search
2.	$S(V_{th}) =$ the set of V_{th} levels to search
3.	$S(\{V_{dd}\}, \{V_{th}\}) = S(V_{dd}) C_{N_{dd}} \times S(V_{th}) C_{N_{th}}$
4.	for each $\{V_{dd}\}, \{V_{th}\} \in S(\{V_{dd}\}, \{V_{th}\})$
5.	remove combinations $(V_{dd}, V_{th}) \in \{V_{dd}\} \times \{V_{th}\}$ s. t. $L_{max}(V_{dd}, V_{th}) < l_{opt}(V_{dd}^{ref}, V_{th}^{ref})$ or $(\frac{P}{T})_{opt}(V_{dd}, V_{th}) > (\frac{P}{T})_{opt}(V_{dd}^{ref}, V_{th}^{ref})$
6.	$\mathcal{S} =$ sorted (V_{dd}, V_{th}) combinations in the ascending order of $L_{max}(V_{dd}, V_{th})$
7.	$P = 0$
8.	$LB = \nu_d^{opt}$
9.	for each $\{V_{dd}, V_{th}\} \in \mathcal{S}$
10.	for $p = 0$ to $\beta - 1$
11.	$T = \min(2\sqrt{N}, (p+1)\nu_{max}(V_{dd}, V_{th}))$
12.	$\perp = \max((p+1)LB, (p+1)\nu_{max}(V_{dd}, V_{th}))$
13.	$P += \int_{\perp}^T \mathbf{R}(\nu) (\frac{P}{T})_{opt}(f, V_{dd}, V_{th}) l_{\beta} \beta d\nu$
14.	$LB = \nu_{max}(V_{dd}, V_{th})$
15.	mark the set $\{V_{dd}\}, \{V_{th}\}$ as optimal if P is the minimum power found

Table 3: Optimal V_{dd} and V_{th} levels search

search, in which the number of combinations for (V_{dd}, V_{th}) grows exponentially as N_{dd} and N_{th} increase. We have found that N_{dd} and N_{th} beyond 3 is impractical from the runtime perspective. Therefore, instead of using large N_{dd} and N_{th} , the power per length function is changed to one which makes use of our $(\frac{P}{T})_{opt}(f)$ function in Section 3.2, and $N_{dd} = N_{th} = 1$. This is equivalent to finding the optimum repeater insertion with computed optimum V_{dd} and V_{th} for each net.

4.2 Experimental Results

The methodology discussed above is used to optimize the full-chip power of chip sizes reported in [1] for various technology generations. N_{dd} and N_{th} are enumerated only up to three for the sake of runtime. V_{dd} and V_{th} search range are minimized without compromising the power optimality. Figure 3 shows the full-chip power of various V_{dd} and V_{th} configurations, where each pair on the x-axis is (N_{dd}, N_{th}) . The highest performance (the most power consuming) combination $(V_{dd}^{ref}, V_{th}^{ref})$ is always retained in all configurations by default, therefore the configuration (1, 1) refers to the optimal full-chip power with fixed reference V_{dd} and V_{th} for all nets. The “ideal” combination refers to the continuous V_{dd} and V_{th} assignment, i.e., $N_{dd}, N_{th} \rightarrow \infty$. Power reduces by 47%, 28% and 13% for 130nm, 90nm and 65nm technology nodes respectively by going from the single V_{dd} , single V_{th} configuration to the dual V_{dd} , dual V_{th} configuration. Using dual V_{th} instead of single V_{th} under dual V_{dd} only gives $\sim 3\%$ power reduction, as opposed to the 20% plus reduction reported for logic circuits in [5]. This suggests that optimizing the single reference V_{th} may just perform as well as the dual V_{th} configuration in terms of power consumption. The dual V_{dd} and dual V_{th} configuration has the total power just 17%, 12% and 5% from the theoretical power optimum configuration which allows infinite V_{dd} and V_{th} levels. Moreover, we observe no significant improvement by moving to combinations with more V_{dd} and V_{th} levels in all technology generations.

The power breakdown of the optimized full-chip interconnect for each (N_{dd}, N_{th}) configuration is shown in each bar in Figure 3. Multiple V_{dd} configurations (i.e., $N_{dd} > 1$) in 130nm and 90nm technology nodes achieve significant dynamic power saving

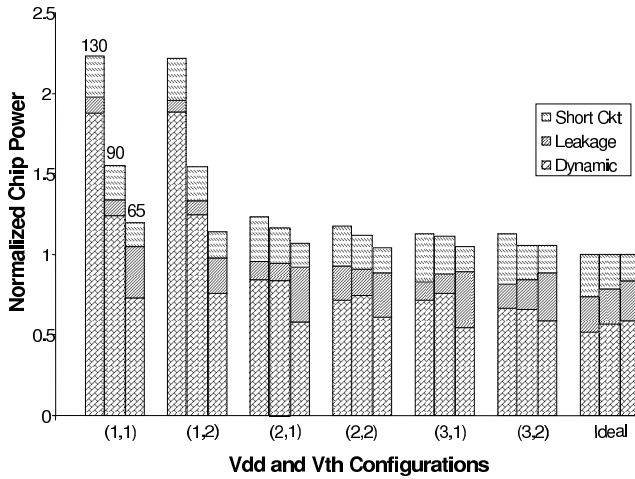


Figure 3: Power of optimized nets under different N_{dd} and N_{th} . Each group of bars contain results for 130nm, 90nm and 65nm technology nodes.

by aggressively reducing the second V_{dd} level, as shown in Table 4. The threshold voltage of the second V_{th} level slightly decreases to compensate for the loss of performance due to V_{dd} reduction, at the expense of slight increase in the leakage power. On the other hand, the leakage power in 65nm technology node is comparatively a lot larger in the (1, 1) configuration. From Table 4, the second $V_{th} = 0.2V$ leaps above the reference level of $0.175V$ to limit the growth of leakage power. This can be seen in Figure 3, where the block of leakage for the 65nm bars slightly reduces from (1, 1) to multi- V_{dd}/V_{th} configurations. Therefore, we conclude that in order to get the right balance between dynamic power and leakage power for total power reduction in interconnect, we must consider both V_{dd} and V_{th} optimization.

Tech Node (nm)	(N_{dd}, N_{th})	V_{dd} s (V)	V_{th} s (V)
130	(2, 1)	1.1, 0.572	0.275
	(2, 2)	1.1, 0.506	0.226, 0.275
90	(2, 1)	1, 0.64	0.25
	(2, 2)	1, 0.64	0.2, 0.25
65	(2, 1)	0.7, 0.532	0.175
	(2, 2)	0.7, 0.532	0.175, 0.2

Table 4: V_{dd} and V_{th} levels for each (N_{dd}, N_{th})

Figure 4 shows the breakdown of total wire length being assigned to (V_{dd}, V_{th}) marked on each region of the figure for the dual V_{dd} , dual V_{th} case. The regions are ordered in the increasing power (the decreasing delay) (V_{dd}, V_{th}) combinations from the bottom to the top. A large portion of the net is assigned to the combination which has V_{th}/V_{dd} ratio way above the default 0.25, particularly for 65 nm technology. This implies that the V_{th}/V_{dd} ratio has to be increased in order to attain power optimality. This is in line with the conclusion made by other works in the literature [9], which suggests that the V_{th}/V_{dd} ratio has to be larger than that current designs use.

5. CONCLUSIONS

This paper studies the opportunity of power saving by computing power optimal repeater sizes, repeater insertion lengths, and for the first time V_{dd} and V_{th} levels for both single nets and a full chip. We have derived a set of analytical formulae which finds the optimal interconnect power given the amount of the timing slack on a single

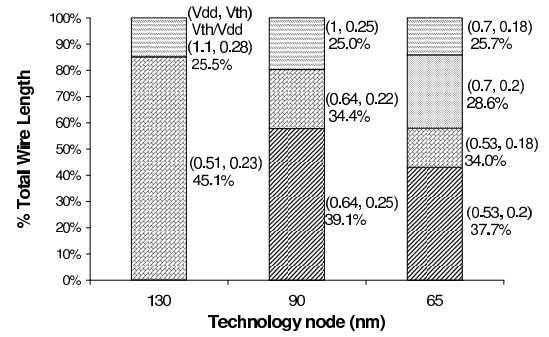


Figure 4: Net length distribution for dual V_{dd} , dual V_{th} configuration

net. Compared to [2] which does not consider V_{dd} and V_{th} as design variables, our method that customizes V_{dd} and V_{th} for each net can reduce power by more than 50% for both single nets and at the chip level. We have also studied the power saving of using multiple V_{dd} and V_{th} levels for buffering interconnects. Power reduces by 47%, 28% and 13% for 130nm, 90nm and 65nm technology nodes respectively by going from the single V_{dd} , single V_{th} configuration to the dual V_{dd} , dual V_{th} configuration. The fact that majority of the nets favors a V_{dd} to V_{th} ratio of more than 0.35 across all generations suggests that the ratio of 0.25 as suggested by other works in the literature is too low for power optimality. We show that the dual V_{dd} and dual V_{th} configuration is within 17%, 12% and 5% of the theoretical optimal power computed from our analytical method for 130nm, 90nm and 65nm technology node; and that extra V_{dd} or V_{th} level beyond dual V_{dd} and dual V_{th} only gives marginal improvement. Our experiment also shows that multiple V_{th} does not improve power of interconnect as much as that of logic circuits.

Our future work focuses on evaluating the suggested system-wide V_{dd} and V_{th} for power optimality of both logic circuits and interconnects. One assumption in this work is that we treat the reference combination $(V_{dd}^{ref}, V_{th}^{ref})$ as always available for nets' selection, while other combinations of V_{dd} and V_{th} are explored. This assumption is reasonable since we assume all other parts of the chip have at least the reference supply and threshold voltage used by logic circuits. However, we may achieve better overall power by re-designing the system power supply and threshold voltages. In the future we will remove such restriction and allow system-wide V_{dd} and V_{th} exploration.

6. REFERENCES

- [1] Semiconductor Industry Association, <http://public.itrs.net>, 2001.
- [2] K. Banerjee and A. Mehrotra, "A power-optimal repeater insertion methodology for global interconnects in nanometer designs," *IEEE Trans. on Electron Devices*, vol. 49, pp. 2001–2007, November 2002.
- [3] G. Chen and E. Friedman, "Low power repeaters driving RC interconnects with delay and bandwidth constraints," in *IEEE International ASIC/SOC Conference*, pp. 335–339, August 2004.
- [4] M. Mui, K. Banerjee, and A. Mehrotra, "A global interconnect optimization scheme for nanometer scale vlsi with implications for latency, bandwidth, and power dissipation," *IEEE Trans. on Electron Devices*, vol. 51, pp. 195–203, February 2004.
- [5] A. Srivastava and D. Sylvester, "Minimizing total power by simultaneous vdd/vth assignment," *IEEE Trans. Computer-Aided Design of Integrated Circuits and Systems*, vol. 23, pp. 665–677, May 2004.
- [6] T. Sakurai and A. Netwon, "Alpha-power law mosfet model and its applications to cmos inverter delay and other formulas," *IEEE Trans. on Electron Devices*, vol. 25, no. 2, pp. 584–594, 1990.

- [7] J. Davis, V. De, and J. Meindl, "A stochastic wire-length distribution for gigascale integration (GSI)–part I: Derivation and validation," *IEEE Trans. on Electron Devices*, vol. 45, pp. 580–589, Mar. 1998.
- [8] J. Davis, V. De, and J. Meindl, "A stochastic wire-length distribution for gigascale integration (GSI)–part II: Application to clock frequency, power dissipation, and chip size estimation," *IEEE Trans. on Electron Devices*, vol. 45, pp. 590–597, Mar. 1998.
- [9] M. Hamada and et al, "A top-down low power design technique using clustered voltage scaling with variable supply-voltage scheme," in *Proc. IEEE Custom Integrated Circuits Conf.*, pp. 495–498, 1998.